# Spatial interpolation of air pollution measurements using CORINE land cover data

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#### Abstract

Real-time assessment of the ambient air quality has gained an increased interest in recent years. To give support to this evolution, the statistical air pollution interpolation model RIO is developed. Due to the very low computational cost this interpolation model is an efficient tool for an environment agency when performing real-time air quality assessment. Beside this, a reliable interpolation model can be used to produce analysed maps of historical data records as well. RIO is an interpolation model that can be classified as a detrended Kriging model. In a first step the local character of the air pollution sampling values is removed in a detrending procedure. Subsequently, the site-independent data is interpolated by an Ordinary Kriging scheme. Finally, in a re-trending step a local bias is added to the Kriging interpolation results. As spatially resolved driving force in the detrending process, a land use indicator is developed based on the CORINE land cover data set. The indicator is optimized independently for the three pollutants  $O_3$ , NO<sub>2</sub> and PM<sub>10</sub>. As a result, the RIO model is able to account for the local character of the air pollution phenomenon at locations where no monitoring stations are available. Through a crossvalidation procedure the superiority of the RIO model over standard interpolation techniques, such as the Ordinary Kriging is demonstrated. Air quality maps are presented for the three pollutants mentioned and compared to maps based on standard interpolation techniques.

# **1** Introduction

Ambient air quality is a major concern in highly urbanized and industrialized regions such as Belgium. For its assessment, a dense network of automatic monitoring sites is implemented by the three Belgian regions, collecting real-time data on a half-hourly basis. The real-time measurements of the telemetric networks<sup>\*</sup> are used to inform the authorities and the public on actual air quality levels, to trigger a warning mechanism in case of threshold exceedance and to feed short term forecast models which predict air quality up to a few days ahead. The average distance between the nearest measuring stations is about 25 km. In spite of this dense coverage, it remains non-trivial to make an accurate spatial map from these point measurement values. However such a map is of great importance to accurately describe the general features of the spatial patterns of air pollution in Belgium, a need which has been put forward by the Belgian Interregional Environment Agency IRCEL. As an additional requirement, the resulting maps have to be available on-line in real time and at a minimal computational costs. This excludes the use of comprehensive time consuming deterministic air quality models for this purpose.

Apart from real time assessments, EU Member States must assess annual ambient air quality in all air quality zones and agglomerations on their territory. As expressed by the EU Air Quality Framework Directive 96/62/EC (EC, 1996) and the 4 emanating Daughter Directives, the actual reporting of this assessment is done - according to the EU Commission Decision 2004/461/EC (EC, 2004) - with the help of a questionnaire listing up the levels and exceedances at the measuring points in order to check compliance with the EU limit and target values. In view of a new Air Quality Directive the Commission tends, in line with the INSPIRE directive 2007/2/EC (EC, 2007), to promote more geographical oriented air quality assessment tools in order to check compliance throughout the zones and agglomerations of the Member States, rather than checking compliance in uplisted data at individual and not always geographically representative points. In this perspective, it is essential for the Environment Agencies of the Member States that they can rely on a tool for the production of correctly analyzed air quality

<sup>&</sup>lt;sup>\*</sup> The telemetric networks are managed by the Flemish Environment Agency (VMM) in Flanders, the Brussels Institute for Management of the Environment (IBGE-BIM) in Brussels and the Institute for Public Service (ISSEP) and the Ministry of the Environment (DGRNE) in Wallonia.

maps. So, an accurate spatial interpolation model is an indispensable vital tool. In the recent literature a number of air pollution interpolation models have been presented (Ross *et al.* 2007, Arain *et al.* 2007, Denby *et al.* 2005). In these papers variants of the Kriging interpolation technique are presented as well as various possibilities for the implementation of land use regression models. These models combine in-situ measurements and auxiliary land use data to produce air quality maps.

Pollutants such as ozone, NO<sub>2</sub> or PM<sub>10</sub> are governed by two different mechanism, each acting on a different spatial scale. On the regional level, fluctuations in the concentration pattern are mainly driven by meteorological (sub-continental) phenomena (Tombette *et al.* 2007, Mensink *et al.* 2007). Beside this, ambient air pollution can have a distinct local character due to local emission sources and their temporal variability (Vautard *et al.* 2007). In an urbanized region such as Belgium, the latter effects are significant (Mensink *et al.* 2005). In this paper we describe an interpolation model, called RIO, that is developed to incorporate both the regional and local aspects of the air pollution phenomenon and that produces concentration estimates on a  $4x4 \text{ km}^2$  grid.

The outline of this paper is as follows. In Section 2 the RIO methodology is described in detail. In Section 3 model results are discussed, validated and compared with standard interpolation techniques. The same section contains a subsection on the uncertainty of the RIO results and outlines the operational setup of the model. A conclusion is presented in Section 4.

# 2 Methodology

The basics of the RIO model are described in depth in the paper by Hooyberghs *et al.* (2006). Here we will briefly resume the outline of the methodology with a focus on the extensions of the RIO model.

### 2.1 Land use patterns and ambient air quality

RIO's fundamental idea is a detrending or removal of the local character of sampling values before they are interpolated. The transformation of the air pollution values into site-independent quantities results in a spatial homogeneous input set which is a prerequisite for a correct use of any interpolation algorithm. Note that this fundamental requirement of spatial homogeneity of the input data if often disregarded in (air pollution) interpolation analyses. After the interpolation step, a re-trending or retransformation is applied in order to incorporate the local character in the final map at places where no monitoring data is available. To deal with the local scale of the air pollution phenomenon, a methodology is developed that links specific (statistical) properties of the air pollution to land use patterns at the same local scale. The methodology results in mathematical relations that establish those links and that can be used in the RIO interpolation model.

In our previous work (Hooyberghs et al. 2006), the driving force (explaining variable) for detrending the measured ozone values was the amount of ozone titration by NO. The strength of the local NO-titration was surrogated by the local population density. However, we have observed that the spatial pattern of population density, although being a good driving force for ozone concentrations, is not necessarily a good and sufficient driving force for other pollutants such as  $PM_{10}$  which are not as exclusively linked to population density as ozone. Therefore, it is expected that the applicability of population density as an explaining variable for the local character of all pollutants (e.g. NO<sub>2</sub>,  $PM_{10}$ ...) is rather limited and should be extended by additional land use information. As such a land use parameter is defined for each pollutant based on CORINE Land Cover (CLC) maps (EEA 1995). By relying on the CLC data set, all different land cover types (urban, industrial, traffic, agricultural, natural,...) can be included in the analysis. The CLC data set provides a high resolution description (100x100 m<sup>2</sup> pixels are used) of the land use patterns, making use of 44 different land cover classes. As will be described in the next section, the CLC description is transformed into a so-called land use indicator, specifically optimized for each pollutant. By doing so, the high dimensionality of the driving force data (44 CLC classes) is reduced to one single value, representative for the local land use characteristics for a particular pollutant. A CLC map of Belgium with the NO<sub>2</sub> monitoring locations in presented in Figure 1. The red-coloured densely populated

regions in the northern and central part of the country are clearly revealed as well as the green coloured rural areas and the large forests in the south.

>>> FIGURE\_1

### 2.2 Land use indicator

In the assessment procedure of the land use indicator, the first step is a characterisation of the land cover in the direct vicinity of the monitoring sites. After all, it is only at those locations that both air pollution concentrations and land use information is at hand and that relations between both can be formulated.

For each monitoring station, a buffer zone dimensioned by a fixed radius is created (see Figure 2). Inside each buffer zone, the CLC pixels (100x100 m<sup>2</sup>) are determined and classified according to the 44 CLC classes. The resulting histogram can be seen as a spectrum that represents a fingerprint of the land use characteristics of the surroundings of the monitoring stations. Figure 3 shows that these land use fingerprints are quite different in the vicinity of a rural, an urban background and an urban station. The radius of the vicinity buffer is a free parameter in the methodology but it turned out that a radius of 2 km produces the best results. When the buffer is chosen too small, it becomes difficult to discriminate between e.g. a small town and a larger city. When the buffer is too large, the site-specific character of the CLC class distribution disappears and the distribution evolves to a general spectrum with very little discriminating power.

>>> FIGURE\_2

>>> FIGURE\_3

### 2.2.1 Establishing the land use indicator ß

In order to reduce the high number of degrees of freedom in the land use description, the 44 CLC classes are grouped into 11 more general land use classes, hereafter called the RIO classes (RCL). The definition of those RIO classes is given in Table 1. Note that

especially for the urban, industrial and traffic classes, the highest resolution of the CLC classes is maintained in the RIO set.

>>>> TABLE 1

In order to define a single value indicator that correlates the local land use characteristics to the local air pollution levels, the RIO class distribution in the vicinity of the station is transformed into a single land use parameter  $\beta$ , according to the relation:

$$\beta = \log \left[ 1 + \frac{\sum_{i} a_{i} \cdot n_{RCLi}}{\sum_{i} n_{RCLi}} \right], \tag{1}$$

In this formula, the index *i* runs over all RIO classes.  $n_{RCL i}$  is the number of pixels of class *i* inside the buffer and  $a_i$  is a pollution related coefficient for the RIO class *i*. As such, the  $\beta$ -parameter is the logarithm of a weighted and normalised sum of the RIO class distribution. The pollution related coefficients  $a_i$  are used to weigh the importance of a particular RIO class on the concentration in the air of the pollutant under investigation. The  $\beta$ -indicator can then be optimized for each pollutant individually by choosing a best set of  $a_i$  coefficients for the RIO-classes as will be described in Section 2.2.2 and Section 2.2.3.

#### 2.2.2 First guess of the land use indicator ß

A zero value for a particular  $a_i$  coefficient in Eq. (1) means that the corresponding RIO class *i* is of no importance for the determination of the pollutant concentration in that area. Generally this might be the case for the RIO classes RCL10 and RCL11 which correspond to rural or natural land and water bodies. The RIO class RCL2 on the other hand (discontinuous urban fabric) can be considered as a land use type of major importance for the air pollution. Its corresponding coefficient  $a_2$  can be set at a reference value of 1 for normalisation purposes. By fixing the  $a_i$  coefficients for RIO classes RCL10 and RCL11 at zero and for class RCL2 at the value of 1, the  $\beta$  parameter is forced to glide between 0 and an acceptable upper value (somewhere below 2). Moreover, by

setting and keeping three out of the 11  $a_i$  values at fixed values, the number of degrees of freedom for the parameterisation of the  $\beta$ -value (Eq. 1) is reduced from 11 to 8.

A numerical procedure will further on optimize the 8 remaining  $a_i$  coefficients. However, a detailed analysis pointed out that the optimal solution is sensitive to the initial guess of the  $a_i$  set. As can be expected, this optimal set is probably only a local minimum in an 8 dimensional parameter space. In order to avoid finding in a irreproducible way a local minimum as an optimal set in the optimization, the procedure should start from a well founded air quality related initial guess for the  $a_i$  coefficients. For this we rely on the distribution over the 11 EMEP sectors (EMEP, 2007) of the Belgian national air pollution emission data. To do so, a pragmatic relation between the 11 EMEP sectors and the 11 RIO classes was needed. The relations are presented in Table 3 together with the corresponding Belgian emission totals of NO<sub>x</sub> and PM<sub>10</sub> for the year 2004.

In order to transform emission data into  $a_i$  coefficient values and still keeping the already fixed values of zero for the  $a_{10}$  and  $a_{11}$  coefficients as well as the reference value of 1 for the  $a_2$  coefficient, the sector emission data are normalised with respect to the RCL2 values. In this way a justified set of  $a_i$  coefficients is obtained which can be used as initial guess for a reproducible  $\beta$ -optimisation procedure for each pollutant. The NO<sub>x</sub> set is used as start value for both O<sub>3</sub> and NO<sub>2</sub> since both pollutants are strongly correlated through atmospheric photochemistry.

>>>> TABLE 2

Based on the first guess parameterisation of the  $\beta$ -parameter, a  $\beta$ -value can be assigned to each air quality monitoring station. The corresponding values give an indication of the land use characteristics in the direct vicinity of the sampling site and will be used to classify the sites.

### 2.2.3 Optimization of the land use indicator ß

Once the stations are characterised by a  $\beta$ -value, we can try to formulate the relations between land use and air pollution properties. Therefore, the long term average of the

pollutant value in each monitoring station is plotted versus the corresponding  $\beta$ -value of the station. This plot represents what will be called further on the "trend" function: it is the correlation between the mean pollutant value and the land use  $\beta$  parameter for the near vicinity (e.g. see Figure 4). In this analysis a time averaging period from 2001 to 2006 is used for all pollutants.

So far, the  $\beta$  value is determined by the first guess parameterisation of the RIO class distribution. At this stage, it is essential to first optimize this parameterisation for each pollutant individually. This can be done by optimising the correlation between the average air pollution value and the  $\beta$  parameter. Indeed, a perfect (or high) correlation between the average air pollution values and the  $\beta$  parameter can be understood as an optimal parameterisation of the local character of the spatial distribution of the air pollution. Here, the optimization is obtained by minimizing the RMS error of a 2<sup>nd</sup> order polynomial fit. For the numerical optimisation a Generalized Reduced Gradient nonlinear optimization code is used, standard available in a numerical software package. Based on the initial guess values formulated in Section 2.2.2, optimal solutions were identified for O<sub>3</sub> and NO<sub>2</sub>. For PM<sub>10</sub> the solver did not find the best solution automatically. With some minor manual corrections and by further optimizing only a subset of the  $a_i$  set, a slightly lower RMSE value for the fit could be identified. However, in general we can conclude that the procedure for the initialisation of the  $a_i$  parameters was successful and gives rise to acceptable results which can easily be reproduced. The resulting optimal weights  $a_i$  for the  $\beta$  parameterisation are summarized in Table 3.

The  $2^{nd}$  order polynomial fit that is obtained in the optimization procedure can be used as a mathematical expression for the trend function describing the land use – air quality relations. If the polynomial fit turns out to be non-monotone (e.g. Figure 4 – right panel), a constant level is imposed for the lower/higher  $\beta$ -values to describe the plateau which is reached. As an alternative, an asymptotic exponential function can be used to describe the trend. In a cross check analysis it was concluded that this alternative function gives similar results.

>>>> TABLE 3

Based on the optimized  $a_i$  parameters, a  $\beta$ -indicator can be calculated for each monitoring station and for each type of pollutant separately and a corresponding best fit for the trend function is obtained. Results for the summer average of the maximum daily 1h ozone values are presented in Figure 4 where the average is given separately for week and weekend days. As becomes clear from the plots, a clear trend can be observed for the average daily maximum ozone value as a function of the  $\beta$ -parameter. This figure also indicates the well known characteristics of the ozone phenomenon in Belgium, which is typical for regions with a high population and traffic density (Vanderstraeten 1996). For low  $\beta$ -values (in rural areas) average ozone values are high and equal for week and weekend days. For high  $\beta$ -values corresponding to urban or industrialized regions, lower average ozone values are observed and much more difference is revealed between week and weekend days. This phenomenon can be explained by the so called "NO titration effect". This effect is known for a long time (Jiménez *et al.* 2005, Sillman 1999) and was also already described by Hooyberghs *et al.* (2006).

For NO<sub>2</sub> the mean values show a more intuitive behaviour with respect to the  $\beta$ -values. This is presented in Figure 5 where higher daily maximum values are observed for highly urbanised or industrialized locations. Note that also here a difference is observed between week and weekend days. The results for PM<sub>10</sub> are presented in Figure 6. From this plot it is clear that PM<sub>10</sub> shows the weakest relation of the three pollutants considered in this study. This is not a complete surprise, since PM<sub>10</sub> is a rather erratic pollutant with many unknown or poorly characterized emission sources (Fuller *et al.* 2004, Almeida *et al.* 2005) and complex secondary formation processes (Sillanpää *et al.* 2006).

>>> FIGURE\_4

>>> FIGURE\_5

>>> FIGURE\_6

### 2.2.4 ß land use indicator maps

Up to now the optimized parameterisation of the  $\beta$ -indicator was applied to establish the land use indicator in the vicinity of the monitoring sites. However, the  $\beta$ -indicator can also be calculated on a regular grid for the entire territory of the country. To obtain such a gridded  $\beta$ -map on the base of the CLC map shown in Figure 1 the contribution of each RIO-class (or equivalently CLC) is calculated in each grid cell and subsequently converted into a unique  $\beta$ -value according to the definition in Eq. (1). The resulting  $\beta$ maps for ozone,  $NO_2$  and  $PM_{10}$  are presented in Figure 7. The plots in this figure indicate the similarities and the differences in the general spatial distribution pattern of the three air pollutants. The spatial distribution pattern of ozone and NO<sub>2</sub> are rather similar. This can be explained by their strong (but opposite) relation to NO<sub>x</sub> emission sources in urbanised and industrialised areas. It must indeed be repeated that due to the NO-titration effect, high  $\beta$ -values in the ozone map correspond to low ozone concentrations whereas the opposite is true for NO<sub>2</sub> concentrations. In the  $\beta$ -map for PM<sub>10</sub> the major urbanised regions are recognised as well but higher  $\beta$ -values are now also observed in some rural areas of the country. Those regions are characterised by important agricultural activities which have an non-negligible impact on the  $PM_{10}$  formation due to primary emissions and emissions of PM<sub>10</sub> precursors such as NH<sub>3</sub> (Erisman et al. 2004, Pinder et al. 2007, Mensink et al., 2007).

>>> FIGURE\_7

In the CLC data set, traffic is available as an individual class given that this is the dominant land use in the  $100 \times 100 \text{ m}^2$  pixel. It turns out that only a small fraction of the total number of pixels can be attributed to a pure traffic class. Nevertheless, the effect of traffic is expected to be large in the vicinity of the major highways, in particular for NO<sub>2</sub>. To upgrade the current RIO methodology a combination of CLC information and traffic volumes was tried out to deduce a more complex  $\beta$ -parameter along the same lines as presented above. It turned out that the addition of an optimized traffic term contributed to the NO<sub>2</sub>  $\beta$ -values for some 5% as an average over all grid cells, although for some cells the contribution was more important. For ozone and PM<sub>10</sub> no contribution at all was observed after the optimisation procedure. From this analysis it can be concluded that

most of the information of traffic impact on ambient air quality levels is already contained in the CLC data set.

### 2.3 Detrending of measured values

So far, only trend functions for the mean values of the pollutant concentration at the measuring sites are presented. However, similar trends can be established for the variance or standard deviation of the time series of the monitoring data (Figure 8). A net trend is observed for the standard deviation of the distribution of  $NO_2$  and  $PM_{10}$  values. As a consequence it can be concluded that also the variance in those  $NO_2$  and  $PM_{10}$  concentration values depends on the land use. For ozone, it turns out that the variance is rather independent of the land use characteristics.

>>> FIGURE\_8

The basic idea of the RIO model is to apply those relations (for both the mean values and standard deviations) in a detrending procedure of the air quality sampling values. This detrending procedure is an essential step to obtain spatial homogeneity of the sampling values before they are used in the interpolation scheme. The detrending step is schematically depicted in Figure 9. According to a station's  $\beta$ -value, a theoretical shift  $\Delta C$  is calculated as the difference between an arbitrary reference level (in the case of NO<sub>2</sub> this is 70µg/m<sup>3</sup>) and the trend function. This residue  $\Delta C$  is then added to the sampling value to establish the detrending. By doing so, the local character of the monitoring data is removed and all values are transformed to a site-independent ( $\beta$ -independent) reference level. Of course, local differences between the various monitoring sites still exist in the detrended sampling values (as they were already present before detrending) due to local variability of the general air quality pattern over the region.

>>> FIGURE 9

The detrending of the mean value is performed by a simple linear translation as presented in Figure 9. As mentioned above, for some of the pollutants a clear trend is also observed in the standard deviation of the monitoring time series. In order to remove also the discrepancies in the variances of the sampling data at different locations, a detrending (or rescaling) is also applied for the standard deviation according to the transformation:

$$x_{\rm det} = \left(x - \langle x \rangle\right) \frac{\sigma_{\rm ref}}{\sigma(\beta)} + \langle x \rangle \tag{2}$$

where  $\sigma_{ref}$  is the reference level of the detrending,  $\sigma_{\beta}$  is the theoretical standard deviation corresponding to the local  $\beta$ -value of the station and  $\langle x \rangle$  is the overall mean of the time series. This transformation ensures a reshaping of the data to obtain an uniform standard deviation  $\sigma_{ref}$ . The result of the detrending procedure for two typical stations is presented in Figure 10. From those graphs it becomes clear that initially both stations have a totally distinct character and distribution. Those differences are almost completely removed after the detrending operation. An overall appreciation of the quality of the detrending procedure can be obtained from Figure 11, where the mean values and standard deviations for all NO<sub>2</sub> stations are presented before and after the detrending procedure. From this figure, it is clear that a large part of the local character of the measurement time series is removed by the detrending, both in the mean value and the variance of the probability density. This is a crucial achievement in the RIO methodology.

>>> FIGURE\_10

>>> FIGURE\_11

### 2.4 Kriging interpolation of detrended values

The interpolation routine of RIO is based on an Ordinary Kriging scheme (Isaaks *et al.* 1989). This technique was originally developed in geostatistics but has proven to be successful in other domains as well (Van Leeuwen *et al.* 1996, Denby *et al.* 2005). The Kriging technique which is used in this work differs from the standard technique on one important point. In standard Ordinary Kriging the variogram or spatial correlation

function is solely determined on the basis of the input values of the interpolation problem at hand. However, for air quality interpolation problems the number of input values for a particular situation (e.g. a 1 hour averaged real-time data set) is rather limited. For a country such as Belgium, typically 50 sampling sites are available. This limited number of sampling values can compromise the statistical significance of the correlation function or variogram. Moreover, air pollution sampling values can be subject to rather large variations on a 1 hour time step. As a result, the correlation function will be subject to the same (erratic) variations. To tackle this problem and to improve statistics, the correlation functions in RIO are constructed on the basis of the entire historical set of measurement time series. In this way a larger data set over different years can be used for the construction of the correlation function. In addition, this procedure allows for a unique correlation function for each time averaging value that is to be calculated by the interpolation model. Correlation functions can be constructed for e.g. maximum 1-hour values, for daily mean values, for maximum daily 8-hour mean values or for each specific hourly value in the day. The correlation functions are not calculated for week and weekend days separately as was done for the trend functions. In a cross check only minor differences were observed when both data sets are handled separately. This is because the correlation functions are established on the base of already detrended time series where week and weekend days differences are already levelled out since both data sets are transformed to the same reference level.

Examples of the spatial correlation functions are given in Figure 12 and Figure 13. The points in the plots represent the correlation values defined as the covariance of two time series in a pair of two detrended monitoring stations, separated by a distance r. The red lines in the plots represent the best (exponential) fit and are used as a spatial correlation function in the Kriging interpolation scheme.

From Figure 12 it is clear that a significant difference is observed between the three pollutants. It turns out that (detrended) ozone is highly correlated, up to very long distances. For  $PM_{10}$  and  $NO_2$ , much more scatter is observed in the spatial correlation plots and correlation functions with a shorter range are obtained.

>>> FIGURE\_12

As stated before, the RIO methodology can be applied for any time aggregation value. Therefore, the correlation functions are also derived for each hourly value in the day. For ozone, the results are presented in Figure 13 and similar results are obtained for  $NO_2$  and  $PM_{10}$ . In this plot, it can be noticed that for morning and evening ozone values the spatial correlation is rather low. For ozone values in the (late) afternoon high correlations are observed in agreement with the maximum 1-hour correlation function in Figure 12.

>>> FIGURE\_13

## 2.5 Re-trending the Kriging results

When the Kriging interpolation of the detrended air quality values is performed, a subsequent re-trending procedure has to be performed in order to restitute the impact of the local land use characteristics in each spatially interpolated point. This re-trending is carried out by making use of the specific  $\beta$ -value of the interpolation grid cell (see Figure 7 for the  $\beta$ -maps). Based on this grid cell specific  $\beta$ -value a concentration shift  $\Delta C$  can be determined as the difference between the reference level and the trend function. This concentration residue  $\Delta C$  is then subtracted from the grid cel concentration value obtained in the Kriging interpolation. The procedure re-introduces the local character in the concentration level. The general idea of the re-trending is presented in Figure 14. Although not presented in this figure, a re-scaling of the Kriging map is also applied in order to restore the scaling transformation as presented in Eq. (2).

>>> FIGURE\_14

# 3 Results and discussion

# 3.1 Model validation

In this section the performance of the RIO interpolation model is examined in a so called jack-knife or cross-validation analysis making use of the "leaving-one-out" principle. For one particular station each value in the historical time series is recalculated making use of all available monitoring data at that time step except the sampling value of that particular station. This procedure is repeated for the entire time series and for every monitoring station. The years 2003 – 2006 are used as a fixed time period in this analysis. As a validation procedure, the interpolated time series obtained in this way can then be (statistically) compared to the genuine measured values. Here, the quality of the model results is expressed by the Root Mean Square Error (RMSE), the bias and the Mean Absolute Error (MAE).

In order to further evaluate the overall performance of the RIO model, RIO results are compared to two standard interpolation techniques. For this purpose, a fourth power Inverse Distance Weighting (IDW) interpolation scheme is applied together with the Ordinary Kriging (OK) interpolation methodology as available in e.g. commercial GIS packages. The IDW scheme is retained in this analysis since it was commonly used in the past as the standard technique for the production of air quality maps. For the Ordinary Kriging, the special RIO technique of detrending before Kriging and re-trending afterwards is not applied. Furthermore the correlation functions as described in Section 2.4 are not applied but a unique variogram is determined for each time step based on the spatial distribution of the corresponding input values.

Figure 15 presents the results of the cross-validation with the OK and RIO model for ozone. From the figure it is clear that the OK model produces larger RMSE values in the majority of the sampling sites compared to the RIO model. Thereby, the RIO model results are in general less biased compared to the standard interpolation technique. Similar validation results are presented for  $NO_2$  and  $PM_{10}$  in Figure 16 and Figure 17, respectively. With the exception of a few monitoring locations, the performance of the RIO model is in almost all monitoring stations better than the standard technique.

Averaged RMSE, bias and MAE values over all available Belgian monitoring locations are summarized in Table 4. It is clear from the table that RIO outperforms the standard interpolation techniques as for each of the three pollutants the three quality indicators (RMSE, bias and MAE) improve. These RMSE correspond to rather accurate estimates (relative errors of 11% O<sub>3</sub>, 26% NO<sub>2</sub>, 28% PM<sub>10</sub>) which can clearly compete, as far as accuracy is concerned, with the results of much more sophisticated deterministic models used for air quality assessments (Van Loon *et al.* 2007, Vautard *et al.* 2007) >>> TABLE 4

>>> FIGURE 15

>>> FIGURE 16

>>> FIGURE\_17

### 3.2 Interpolation maps

In this section, the performance of the interpolation model is not evaluated on a statistical basis as in the previous section, but by means of actual annual air quality maps for 2006 obtained with the two different interpolation techniques. The maps of the annual mean are obtained by an hour by hour interpolation of all available (hourly) measurements in 2006. Then, for each pixel in the final map all hourly results are averaged over the year. Note that in this hour-by-hour interpolation RIO is using the hourly parameterisations as derived in the statistical analysis (see Figure 13 in §2.4).

In Figure 18 the annual mean ozone maps for the year 2006 are presented for both the RIO and Ordinary Kriging interpolation techniques. A comparison of the two maps clearly shows the strength of the RIO interpolation scheme as it is able to introduce land use based local variations in the ozone concentrations fields at places where no monitoring data is available. Whereas standard techniques have to rely only on the monitoring data themselves and their relative distances and correlations.

Similar maps for the 2006 annual mean of  $NO_2$  and  $PM_{10}$  are presented in Figure 19 and Figure 20. For  $NO_2$ , the difference between the Ordinary Kriging map and the RIO map

is even more pronounced. This is due to the fact that a great deal of the NO<sub>2</sub> monitoring stations is located in urbanised or industrialized areas, more than it is the case for the ozone sampling sites. As a consequence, a standard interpolation technique extrapolates these enhanced NO<sub>2</sub> levels from the urban sites to the rural areas. RIO is able to deal with these urban stations in a much more accurate way by limiting the high values to only those areas with an urban character. The same conclusions can be drawn for the PM<sub>10</sub> maps. Here, the effect is even more explicit than for the NO<sub>2</sub> case. It turns out that almost all of the PM<sub>10</sub> sampling sites operational in 2006 can be classified as urban, industrial or traffic stations. Based on those measurements only, PM<sub>10</sub> pollution over a large part of territory of Belgium would be assessed according to these enhanced PM<sub>10</sub> levels. Based on the RIO model, the high PM<sub>10</sub> levels are restricted to the urbanised regions, whereas lower levels are introduced in the rural areas. This result radically changes the outcome of any assessment of the exposure of population or area to high concentration values such as exceedances of the European limit values.

>>> FIGURE\_18 >>> FIGURE 19

>>> FIGURE\_20

## 3.3 Uncertainty

When interpolation maps are used for air quality assessments, it is important to have an idea of the uncertainty of the presented maps. Therefore the errors introduced by the RIO interpolation scheme are further explored in this paragraph.

## 3.3.1 Kriging error

When solving the Ordinary Kriging equations, a value for the error variance can be obtained at the same time (Isaaks *et al.* 1989). This error variance  $\sigma_R^2$  is a measure for the uncertainty (1  $\sigma_R$ ) of the interpolation result. The parameters that determine the spatial pattern of  $\sigma_R^2$  are obtained by the Kriging solution. The overall scale of  $\sigma_R^2$  is fixed by

the variance  $\sigma^2$  of the so-called random function model which is the only quantity that needs to be specified. A most obvious choice would be to take the average of the variances of the time series obtained in the different monitoring stations over the country. This choice would be acceptable if, and only if spatial patterns of air pollution around all monitoring stations would be homogeneous. However, due to local and regional pollution sources and sinks, the air pollution phenomenon does not obey at all the necessary requirement of spatial homogeneity and as a consequence, a unique variance  $\sigma^2$ , representative for any location can not be used. To tackle the problem, a β-depended variance  $\sigma^2(\beta)$  will be introduced in the  $\sigma_R^2$  calculation, based on the trend analysis of the variance as presented in Figure 8. These plots indicate that the variance is positively correlated with the  $\beta$ -parameter and that (with an exception for ozone) increased  $\beta$ -values correspond to increased  $\sigma$ 's. This dependency and the fact that  $\sigma^2(\beta)$  is now used as a scaling factor for  $\sigma_R^2(\beta)$  makes that for regions with a low  $\beta$ -value, the Kriging interpolation error is smaller compared to a result that would have been obtained with a unique  $\sigma$  averaged over all stations whereas in urbanised and industrialised regions, characterised by higher  $\beta$ -values, the Kriging error is higher.

#### 3.3.2 Re-trending error

Besides the error due to the Kriging interpolation scheme, an error is also introduced by applying the "trend function" during the re-trending procedure. As this trend function is only a best estimator for the  $\beta$ -dependency of the pollution data (see Figure 21), the use of it during re-trending gives rise to an additional uncertainty. Therefore the error on the polynomial fit through the scattered data is used as an additional and cell specific error term  $\sigma_{trend}(\beta)$ .

>>> FIGURE\_21

#### 3.3.3 Total error map

The total error attributed to the final RIO interpolation result is then calculated as:

$$\sigma_{tot}(\beta) = \sqrt{\sigma_R^2(\beta) + \sigma_{trend}^2(\beta)}, \qquad (3)$$

where both the Kriging error  $\sigma_R(\beta)$  and the error introduced by applying the trend function  $\sigma_{trend}(\beta)$  are taken into account.

As an illustration Figure 22 presents a relative error map for a maximum 1-hour NO<sub>2</sub> map of a particular day. Low interpolation errors (~18%) are found in the vicinity of the monitoring stations whereas higher values (~25%) are found far away from any sampling site. This typical circular error pattern is predominantly caused by the Kriging error. This pattern however is locally distorted according to the corresponding land use characteristics introduced by the  $\beta$ -dependencies of both error terms in Eq. (3). It is interesting to note that the relative higher errors in the North-eastern part of the country are caused by the fact that for the three monitoring stations in this region no valid measurement values were present for this particular day. When measurement data is available in this region, the error values are further reduced.

>>> FIGURE 22

As a closing remark it must be said that the introduction of a supplementary driver (deand re-trending) on top of the Ordinary Kriging for the spatial interpolation, slightly increases the overall total error on the final result. This disadvantage however is largely compensated by the benefits of a much more reliable spatial prognosis obtained in the RIO scheme by introducing the de- and re-trending intelligence, as it is driven by the nature of the pollution itself.

## 3.4 Operational application

From the viewpoint of applicability it is emphasised again that RIO is able to describe different time aggregation values of one pollutant. For the Belgian Interregional Environment Agency (IRCEL) daily maximum 1-hour values, maximum daily 8-hour means and daily mean values are implemented in the model code together with the possibility of an hour by hour interpolation of a set of (real time) hourly sampling values. This latter option allows maximal flexibility and the possibility for calculation of any time aggregation value over any time window from a one hour map up to a map of annual mean concentrations. The former types of maps are published in real time on-line on the website (www.irceline.be) in order to visually inform the authorities and the public about the current and forecasted air quality levels. The latter is used for assessing air quality levels and checking the compliance with limit and target values within the context of the reporting obligations in the EU directives.

Finally it is stressed that the computational cost of RIO is by no means comparable to deterministic air quality models. The Fortran code of the RIO model produces air quality maps on a standard PC within two seconds. This extremely low computational time (compared to deterministic air quality models) is an important asset for the RIO model in the operational setup at IRCEL.

# 4 Conclusions

In this paper the RIO model is presented as an "intelligent" interpolation model for air pollution data. The model was initially developed for ozone interpolations and population density was used as a spatially driving force. In this work, the model is extended for  $NO_2$  and  $PM_{10}$  and a land use indicator based of the CLC data set is introduced. This new land use indicator (the  $\beta$ -parameter) offers a maximum flexibility in the development of the relations between land use and air pollution levels. Those relations are the core of the RIO model and they are used to remove the local character of the air quality monitoring data before they are used in the interpolation scheme. In the RIO model, a detrending of the monitoring data is applied according to the observed trend in the mean values and the standard deviation. Especially for  $NO_2$ , the latter effect is substantial.

The evaluation of the RIO model in a cross-validation procedure clearly revealed that the new methodology produces better results compared to standard interpolation techniques such as IDW or Ordinary Kriging. The improvements of the RIO model can be attributed to the detrending procedure which is applied on the air quality monitoring data and the re-trending step that is imposed on the Kriging map. It was shown that RIO performed best on the basis of all indicators. In this respect, the small bias values of the RIO model were most striking. Subsequently, the interpolation model was further evaluated based on the resulting maps. It was illustrated that RIO is able to produce local variations in the concentration fields at places where no monitoring data is available. This is because of RIO's ability to incorporate land use information and not just monitoring data. This is especially important if the air quality gradients at the urban-rural interface have to be described.

At present, the RIO model is being extended along the same lines to incorporate  $SO_2$  measurements. Further we will explore the possibilities to use satellite retrievals such as the Aerosol Optical Thickness parameter as a alternative driving force for the CLC  $\beta$ -indicator in the RIO interpolation scheme for PM<sub>10</sub> (Koelemeijer *et al.* 2006).

The accuracy of the RIO model in combination with it extremely low computational cost makes it a valuable tool for the Belgian Interregional Environment Agency IRCEL in their air quality assessments.

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# Tables

RIO	Description	CLC
class		classes
RCL1	Continuous urban fabric	1
RCL2	Discontinuous urban fabric, green and sport	2,10,11
RCL3	Industrial or commercial units	3
RCL4	Road and rail networks and associated land	4
RCL5	Port areas	5
RCL6	Airports	6
RCL7	Mine, dump and construction sites	7-9
RCL8	Arable land	12-14
RCL9	Agricultural areas	15-22
RCL10	Forest and semi natural areas	23-34
RCL11	Wetlands and waterbodies	35-44

Table 1: Definition of the 11 RIO classes (RCL) as a combination of the 44 CLC classes.

Table 2: Pragmatic relation between the RIO classes and the EMEP sectors. Corresponding EMEP emission totals for the year 2004 and their ratio to the RCL2 value. The latter ones will be used as initial guess for the a<sub>i</sub>-parameters in de β-optimisation.

RIO class	Pollutant coefficient <i>a<sub>i</sub></i>	EMEP sectors	Emission totals 2004 [Gg/y]		Rel. emissions with respect to RCL2 ( <i>a<sub>i</sub></i> initial guess)	
			NO <sub>x</sub> PM <sub>10</sub>		NO <sub>x</sub>	<b>PM</b> <sub>10</sub>
RCL1	a <sub>1</sub>	S2	25.84	2.84	1.0	1.0
RCL2	a <sub>2</sub>	S2	25.84	2.84	1.0	1.0
RCL3	a <sub>3</sub>	S3 + S4	71.91	19.18	2.8	6.8
RCL4	$a_4$	S7	133.53	9.33	5.2	3.3
RCL5	<b>a</b> <sub>5</sub>	S8	21.61	23.69	0.8	8.3
RCL6	a <sub>6</sub>	S8	21.61	23.69	0.8	8.3
RCL7	a <sub>7</sub>	S1 + S4 + S5 + S9	66.71	20.41	2.6	7.2
RCL8	a <sub>8</sub>	S10	0.00	3.06	0.0	1.1
RCL9	<b>a</b> 9	S10	0.00	3.06	0.0	1.1
RCL10	a <sub>10</sub>	S11	0.00	0.00	0.0	0.0
RCL11	a <sub>11</sub>	S11	0.00	0.00	0.0	0.0

RIO	Description	<b>O</b> <sub>3</sub>		NO <sub>2</sub>		$PM_{10}$	
class		ai	frac.	ai	frac.	a <sub>i</sub>	frac.
RCL1	Continuous urban fabric	1.01	5.9%	2.71	4.3%	1.16	3.6%
RCL2	Discontinuous urban fabric	1.00	35.4%	1.00	34.2%	1.00	38.9%
RCL3	Industrial or commercial units	1.41	8.6%	1.23	11.2%	2.07	11.2%
RCL4	Road and rail networks	4.30	2.1%	6.12	2.6%	2.23	2.5%
RCL5	Port areas	8.38	0.2%	3.24	4.1%	2.65	2.1%
RCL6	Airports	0.97	0.1%	1.41	0.9%	1.01	1.1%
RCL7	Mine, dump and construction sites	1.96	0.7%	1.58	0.8%	10.99	0.8%
RCL8	Arable land	0.80	13.5%	0.33	10.9%	0.64	10.7%
RCL9	Agricultural areas	0.35	22.3%	0.00	17.7%	0.64	17.1%
RCL10	Forest and semi natural areas	0.00	9.5%	0.00	8.1%	0.00	8.0%
RCL11	Wetlands and waterbodies	0.00	1.7%	0.00	5.2%	0.00	4.0%

Table 3: Optimised set of  $a_i$ -parameters for the  $\beta$  indicator. Parameter values are given for each pollutant. The column *frac*. contains the relative contribution of a RIO class in the buffer zones of all monitoring stations.

Table 4: Model performance indicators for the IDW, OK and RIO model and for the three pollutants  $O_3$ ,  $NO_2$  and  $PM_{10}$ . Values are averaged over all available Belgian monitoring locations. The mean value for the corresponding time averaging value (e.g. max 1h) is given between brackets <X>. All values are in  $\mu g/m^3$ .

model	O <sub>3</sub> (max 1h, summer)			NO <sub>2</sub> (max 1h)			PM <sub>10</sub> (day avg)		
	< 90.9 >			< 54.8 >			< 35.9 >		
	RMSE	Bias	MAE	RMSE	Bias	MAE	RMSE	Bias	MAE
IDW	10.97	-1.70	8.16	18.17	4.74	14.43	12.12	1.70	8.49
ОК	10.37	-0.44	7.66	16.85	1.45	13.11	11.65	1.22	8.05
RIO	9.56	-0.08	6.89	14.45	-0.67	11.23	9.89	0.01	6.98

# **Figures**

Figure 1: CORINE Land Cover map for the Belgian region. NO<sub>2</sub> monitoring stations with label are indicated by the dots. Densely populated and industrialised areas show up as red coloured while rural and forest areas are green.

Figure 2: Monitoring station 43R240 (Engis) with a 2 km radius buffer. CLC describes the land use in the direct vicinity of the monitoring location.

Figure 3: CLC class distribution in the close vicinity of three typical monitoring locations in Belgium (rural, urban background and urban). For each CLC class, the number of pixels inside the station vicinity buffer is indicated.

Figure 4: Trend function for ozone: average max 1h ozone values as a function of the β-parameter of the Belgian monitoring sites. The left panel shows the results for weekdays, the right panel is based on averages over weekend days. Averages are based on the summer values only between 2001 and 2006. Low β-values correspond to rural areas, high β-values to urban or industrialised sites. Stations are labelled according to their type (rural, urban background, urban, industrial and traffic).

Figure 5: Trend functions for NO<sub>2</sub>: same as in Figure 4 but for the average max 1h NO<sub>2</sub> concentrations on weekdays (left panel) and on weekend days (right panel).

Figure 6: Trend functions for PM<sub>10</sub>: same as in Figure 4 but for the daily mean PM<sub>10</sub> concentrations on weekdays (left panel) and on weekend days (right panel).

Figure 7:  $\beta$  land use indicator maps for ozone (left), NO<sub>2</sub> (middle) and PM<sub>10</sub> (right).  $\beta$  values are calculated on a 4x4km<sup>2</sup> regular grid.

Figure 8: Trend functions for the standard deviation: standard deviation of the sampling values (week days only) as a function of the β-parameter for max 1h ozone (left), max 1h NO<sub>2</sub> (middle) and

daily mean PM<sub>10</sub> concentrations (right). The ozone results are obtained from summer data (April until September) only.

Figure 9: Schematic outline of the detrending procedure applied to measurements. The blue dots represent a selection of measurement values. The red squares are obtained after the detrending step. A concentration residue  $\Delta C$  is added to the measured values.  $\Delta C$  is given as the difference between the reference level and the trend function for the appropriate  $\beta$ -value. The trend function is depicted as the solid line, the reference level is given as the dashed red line.

Figure 10: NO<sub>2</sub> max 1h probability distribution for the urban station 41B006 and the rural station 44N050, before (left) and after (right) the detrending procedure.

Figure 11: Mean values (upper panel) and standard deviations (lower panel) of the max 1h NO<sub>2</sub> values in all stations before (green) and after (yellow) the detrending procedure. The reference level used in the detrending is given as the red line. Stations are ordered according to their  $\beta$ -value, rural stations to the left, urban and industrial stations to the right.

Figure 12: Spatial correlation functions for detrended max 1h summer ozone values (left), max 1h NO<sub>2</sub> (middle) and daily mean PM<sub>10</sub> concentrations (right). The spatial correlation function is printed as a solid red line.

Figure 13: Spatial correlation function for hourly ozone values, specifically determined for each hour of the day.

Figure 14: Schematic outline of the re-trending procedure applied to grid cells. The panel left gives the transformation for 4 different grid cells. The red diamons are the result of the Kriging interpolation. The blue triangles are the result of the re-trending step. A concentration residue  $\Delta C$  is subtracted from the Kriging result.  $\Delta C$  is given as the difference between the reference level and the trend function for the appropriate  $\beta$ -value. The trend function is depicted as the solid line, the reference level is given as the dashed red line. The panels on the right give a Kriging map of detrended measurements (1), a map of the  $\Delta C$  residue (2) and the final RIO result (3). Figure 15: RMSE (left) and bias (right) for max 1h ozone values. Results are presented for the RIOmodel (yellow bars) and for standard interpolation technique Ordinary Kriging (green bars). Summer ozone data are used from the 41 ozone monitoring stations in Belgium between 2003 and 2006.

Figure 16: Same as in Figure 15 but for the max 1h NO<sub>2</sub> values. All available data between 2003 and 2006 is used in the validation. Note that the indicators of station 41B003 go beyond the range of the plot.

Figure 17: Same as in Figure 16 but for the daily mean PM<sub>10</sub> values.

Figure 18: Annual mean ozone map for the year 2006 obtained by the RIO model (left) and Ordinary Kriging (right). The small coloured circles on the map represent the ozone monitoring locations and the corresponding annual mean value at that station.

Figure 19: Annual mean  $NO_2$  map for the year 2006 obtained by the RIO model (left) and Ordinary Kriging (right).

Figure 20: Annual mean PM<sub>10</sub> map for the year 2006 obtained by the RIO model (left) and Ordinary Kriging (right).

Figure 21: Trend function (see left panel of Figure 5) with indication of the error boundaries (dashed lines) for max 1h NO<sub>2</sub> concentration as a function of the  $\beta$ -parameter.

Figure 22: Relative error map for a max 1h NO<sub>2</sub> interpolation result. The error is composed of the standard Kriging error where a  $\beta$ -dependent  $\sigma$  is taken into account and an error due to the uncertainty of the trend function.



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